

## SUPPORTING INFORMATION

for

*Electrostatics of nucleic acid folding under conformational constraint*

Peter C. Anthony, Adelene Y.L. Sim, Vincent B. Chu,  
Sebastian Doniach, Steven M. Block, and Daniel Herschlag

### **Contents:**

1. Supporting Experimental Procedures
2. Supporting Figures
3. Supporting Tables
4. Supporting References

## 1. SUPPORTING EXPERIMENTAL PROCEDURES

### *Dumbbell preparation*

The 20R55/4T DNA hairpin<sup>1</sup>, having a 20-bp stem and a thymidine tetraloop, was obtained as part of a PAGE-purified, chemically synthesized oligonucleotide (IDT), sequence 5' -  
atcgagaggggacacggggaaacacc\_GAGTCAACGTCTGGATCCTGTTTTTCAG  
GATCCAGACGTTGACTC\_catcatcctgactagagtccttggc-3', in which each end of the hairpin sequence (uppercase) was flanked by an abasic site ("\_") and 25 additional nucleotides (lowercase). Double-stranded DNA handles were then prepared with single-stranded overhangs complementary to the flanking sequences in order to link the hairpin to beads. A 2,018-bp handle with a 5' overhang and a digoxigenin label at the opposite end was prepared by PCR, using one autosticky primer<sup>2</sup>, one 5'-digoxigenin-modified primer, and the M13mp18 plasmid as the template. A 1,044-bp handle with a 3' overhang and a biotin label at the opposite end was prepared by PCR templated on the pALB3 plasmid, using one primer containing a phosphorothioate bond and one 5'-biotin-modified primer, followed by digestion with lambda-exonuclease<sup>3</sup>. All primers were obtained from IDT, and both handles were gel-purified and ethanol-precipitated. The hairpin was annealed to the handles in STE+ buffer (100 mM NaCl, 10 mM Tris-HCl, 10 mM EDTA, pH 8.0), with all components at ~20 nM, by lowering the temperature from 80 to 25 °C over 30 minutes. The annealing reaction was then diluted 300- or 900-fold in phosphate buffer (100 mM sodium phosphate, 3 mg/mL BSA, pH 7.5) and incubated with 0.6 µm-diameter avidin-coated beads and 0.73 µm-diameter anti-digoxigenin-coated beads (each ~50 pM in phosphate buffer) at room temperature for 1 hour to form dumbbells.

### *Buffers*

Solutions at 40, 100, 200, 500 and 1000 mM of each of five monovalent cations ( $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$ , and  $\text{TMA}^+$ ) were used for hairpin measurements, as well as solutions containing 40 or 200 mM  $\text{K}^+$  and 1, 2, 5, or 10 mM  $\text{MgCl}_2$ . All ionic solutions were buffered with 50 mM MOPS. The first 40 mM of each monovalent cation was added as the hydroxide salt in order to raise the pH to 7.5; the rest was added as the chloride salt. Dumbbells were diluted 1:30 into the working buffer, consisting of the buffered salt solution and 2% (v/v) oxygen scavenger (250 mg/mL glucose, 37 mg/mL glucose oxidase, 1.7 mg/mL catalase), and flowed onto a microscope coverglass. All ionic concentrations stated in this work are for the starting buffered solutions, excluding the 5% dilution and introduction of trace ions (most significantly, 3.3 mM sodium phosphate) resulting from the addition of dumbbells and oxygen scavenger. However, all calculations (*mfold*, Poisson-Boltzmann and HEL) took these effects into account, so that calculation results and experimental data are directly comparable.

### *Numerical data and error analysis*

All experimental values of  $\Delta x$  and  $F_{1/2}$  (see **Figures 3 and 4** and **Tables S4-S8**) are reported as the mean  $\pm$  total uncertainty, which includes the statistical standard error of the mean (calculated by bootstrap analysis) added in quadrature to estimates of systematic uncertainties in the optical trapping assay. The systematic uncertainty in  $\Delta x$  was estimated to be 2%, corresponding to a ~10-15 nm uncertainty in our measurement of the position of the zero-stiffness region (ZSR) of the weak trap. The systematic uncertainty in  $F_{1/2}$  included 5% to account for variation in the trap stiffness measurements made on the same day and changes to these measurements observed over time, as well as the uncertainties in stiffness due to the refractive index of the buffer (~1%) and

the temperature (<1%). As  $\Delta G$  is the product of  $\Delta x$  and  $F_{1/2}$ , all of the uncertainties in  $\Delta x$  and  $F_{1/2}$  are propagated into the uncertainty of  $\Delta G$ .

#### *Generating ensembles of models for Poisson-Boltzmann calculations*

The initial structural models (folded and unfolded) were energy-minimized (Amber 94 potential<sup>4</sup>, allowing only atoms linking the hairpin to the DNA handles to move) to reduce excess bond-length strains, and then randomized using implicit solvent molecular dynamics simulations as implemented in NAB<sup>5</sup>. A time step of 1 fs was used in all simulations, with snapshots taken after every simulated annealing routine (from 500 K to 300 K in steps of 100 K, with 100,000 steps at each temperature). Electrostatics were accounted for by assuming a solvent dielectric constant of 80 (see **Table S2** for a discussion of other methods). For the folded model, only the residues in the loop and those adjacent to the handle fragments were allowed to move, while for the unfolded model, only the handle fragments were fixed (see **Figure 1**). A total of 40 folded and 40 unfolded models were generated, giving 1600 possible pairs of folded-unfolded models. We have made these models available at [http://csb.stanford.edu/~adelene/hairpin\\_pulling\\_electrostatics](http://csb.stanford.edu/~adelene/hairpin_pulling_electrostatics)

#### *Poisson-Boltzmann calculations*

All Poisson-Boltzmann (PB) calculations were done with the Adaptive Poisson-Boltzmann Solver (APBS) 1.1<sup>6</sup>. Coarse and fine mesh grids of  $272 \times 272 \times 1088$  and  $160 \times 160 \times 641$  were respectively chosen, with  $161 \times 161 \times 641$  grid points used (grid spacing of 1.7 and 1 respectively). The center of the hairpin structure was taken as the box center. Varying the box size, grid spacing and box center resulted in ~6% variation of  $\Delta G_F$  and  $\Delta G_U$  for a given  $[M^+]$ , but much larger variation in the absolute values of  $\Delta G_{el}$ . However, trends in  $\Delta G_F$  and  $\Delta G_U$  with  $[M^+]$

were affected in tandem, so that electrostatic trends in  $\Delta G_{\text{el}}$  were consistent across different choices of parameters. Similarly, absolute values of  $\Delta G_{\text{el}}$  varied significantly across the different pairs of folded and unfolded hairpin models while the trends in  $\Delta G_{\text{el}}$  versus  $[\text{M}^+]$  were consistent. These findings support our expectation that the specific details of the atomic models (and hence DNA-solvent dielectric boundary) do not strongly affect the electrostatic dependence of the unfolding energy on  $[\text{M}^+]^{7,8}$ .

The  $\text{Mg}^{2+}$  titration in 200 mM  $\text{K}^+$  was slightly more sensitive to the box size due to the small calculated changes in  $\Delta G_{\text{el}}$ . In this titration, a non-physical decrease in hairpin stability was observed going from 0 to 1 mM  $\text{Mg}^{2+}$  – a likely numerical artifact we were able to remove by adjusting the grid spacing to 2 Å.

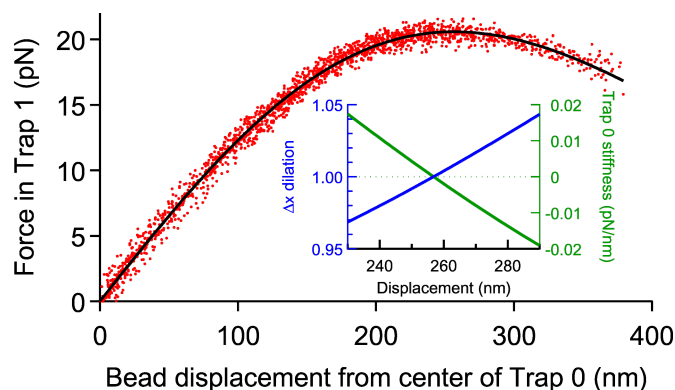
For all calculations, the solvent and DNA dielectrics were set to 78.54 and 2 respectively, and the solvent-accessible probe was 1.4 Å. All ionic “radii” in APBS were set to 2 Å. However it is important to note that PB treats all ions as point charges, and the “radius” parameter only determines the distance of closest approach of the ions to the DNA. Increasing this distance to match the hydrated radius of each monovalent ion (see **Figure S5**) did not consistently improve the fit of the calculated  $\Delta G_{\text{el}}$  trend to the corresponding  $\Delta G$  series (data not shown).

A size-modified version of Poisson-Boltzmann theory was also used to calculate separate  $\Delta G_{\text{el}}$  trends for each monovalent ion except  $\text{TMA}^+$ . The calculations were conducted using an in-house modified version of APBS<sup>9</sup>. In these calculations,  $\text{Na}^+$  (with radius  $a$ ), the predominant trace ion present in all measurements (see “Buffers”), was included at its final diluted concentration as the background cationic species. The titrated ionic species was then included with volume  $(ak^{1/3})$ , where  $k$  is a factor that scales with its parameterized volume<sup>9</sup>.

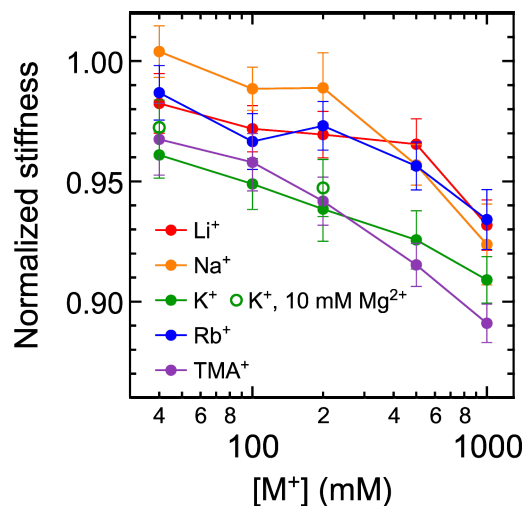
*Fitting Poisson-Boltzmann calculations to experimental data*

As we could not calculate non-electrostatic contributions to  $\Delta G$  with PB, we fitted calculated values of  $\Delta G_{el}$  to our experimentally measured  $\Delta G$  values to assess the ability of PB to capture electrostatic trends. Each calculated  $\Delta G_{el}$  series, corresponding to one pair of folded and unfolded hairpin models, was fitted to the appropriate experimental series by chi-squared minimization with one free parameter (the offset on the energy scale). The averages of the fitted points are plotted in **Figures 3, 4, and S6**. For the  $Mg^{2+}$  titrations, there were minimal changes in  $\Delta G$  between 5 and 10 mM  $Mg^{2+}$  for both background  $K^+$  concentrations, and only points corresponding to these  $Mg^{2+}$  concentrations were used to perform the fitting (**Figure 4A**). We also fit lin-log lines to each monovalent  $\Delta G_{el}$  series, and the slopes (mean  $\pm$  standard deviation) are reported in **Tables 1, S2 and S3**.

## 2. SUPPORTING FIGURES

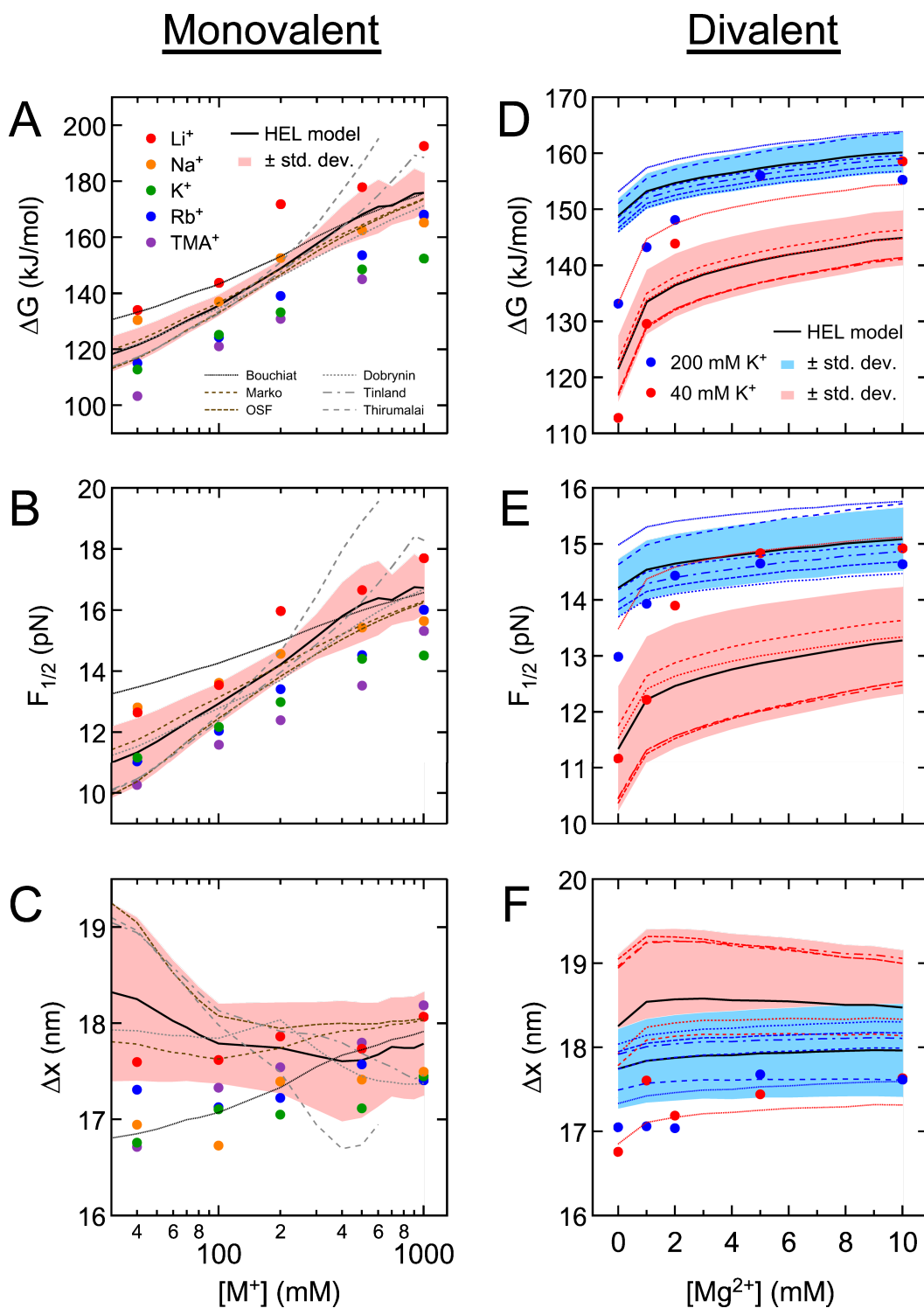


**Figure S1. Calibration of the optical force clamp and correction of measured  $\Delta x$  values.** A dumbbell comprised of two beads joined by a DNA tether was trapped in 200 mM  $K^+$  working buffer. Data (red) were obtained as the traps were separated, with the intensity of Trap 0 set to approximately half that of Trap 1. The data were well-fit by the derivative of a Gaussian function (black), and the peak of this function, corresponding to a bead displacement of approximately 258 nm from the center of Trap 0, was interpreted to be the point at which the stiffness of Trap 0 vanished. The  $\sim 50$  nm region centered on this point was operationally defined as the zero stiffness region (ZSR)<sup>10</sup>. The derivative of the fit function (equal to local stiffness of Trap 0, *inset*), the calibrated stiffness of Trap 1 (0.24 pN/nm), and the stiffness of the DNA construct ( $\sim 0.5$  pN/nm, typical of hairpin force-extension curves measured in this study) were used to calculate<sup>10</sup> the dilation of measured  $\Delta x$  values (*inset*) as a function of displacement. This quantity represents the measured  $\Delta x$  normalized to the true molecular  $\Delta x$ , and was used to rescale measured  $\Delta x$  values to remove the displacement-dependent effect of non-zero Trap 0 stiffness. To ensure that each  $\Delta x$  value was correctly rescaled for the Trap 1 stiffness at which the hairpin molecule was measured, the data (red) were rescaled, the fitting was repeated, and the  $\Delta x$  dilation function was recalculated for each calibrated Trap 1 stiffness used in this study (0.24-0.29 pN/nm).



**Figure S2. Relative trap stiffnesses measured by the method of Brownian fluctuations in working buffers used for data collection.** The stiffnesses were normalized to that measured in water and used to rescale the absolute calibrated trap stiffnesses (and therefore measured  $F_{1/2}$  values) for changes due to the refractive index, which depends on solute concentration. Points for monovalent buffers are connected to guide the eye. Stiffnesses measured for 40 or 200 mM  $K^+$  were not significantly lower in the presence of 10 mM  $Mg^{2+}$  than in the complete absence of  $Mg^{2+}$ . Therefore stiffnesses were not measured in the remaining buffers used for the divalent titrations. Each point represents the mean of at least 10 measurements (each a separate bead)  $\pm$  the standard error.



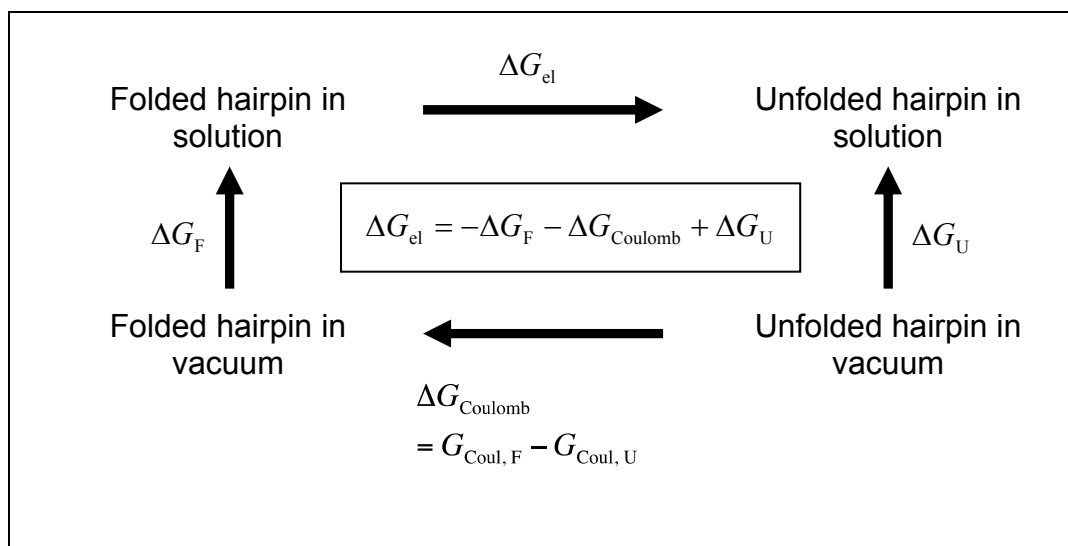


**Figure S3. HEL model calculations separated by persistence length formulation.**  
(Caption on next page.)

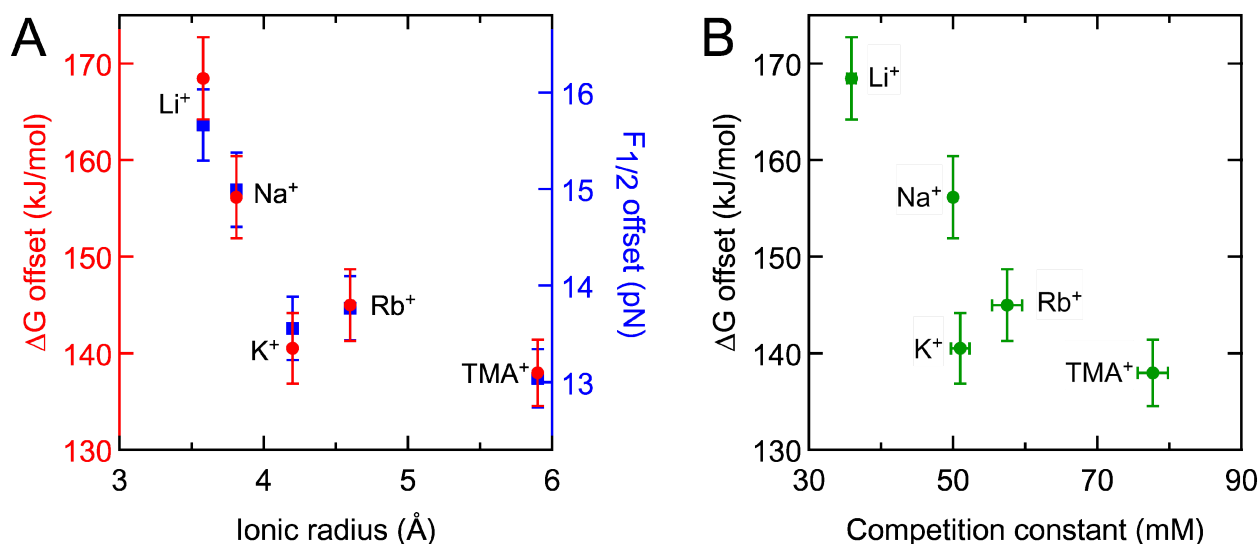
The dependence of ssDNA persistence length ( $L_p$ ) on ion concentration is controversial, and so we ran the HEL model using six different formulations of  $L_p$ :  $L_{p1}$ , the “bare” persistence length from Bouchiat’s approximation to the WLC solution<sup>11</sup>;  $L_{p2}$ , the Odijk-Skolnick-Fixman electrostatically enhanced persistence length ( $L_{p2} = L_{p1} + l_{OSF}$ , where  $l_{OSF}$  is as defined in refs 12,13);  $L_{p3}$ , a scale-dependent persistence length suggested by Marko that is intermediate between  $L_{p1}$  and  $L_{p2}$  ( $L_{p3} = L_{p1} + l_{OSF} \cdot K(q)$ , where  $K(q)$  is as defined in refs 14,15 and  $q$  satisfies the equation  $L_{p3} \cdot q^2 = \text{force}/k_B T$ )<sup>16</sup>;  $L_{p4}$ , as defined by Ha and Thirumalai for flexible polyelectrolytes in the large-screening limit<sup>17</sup>;  $L_{p5}$ , the electrostatic persistence length defined by Dobrynin<sup>18</sup>; and  $L_{p6}$ , an empirical, force-independent and ionic strength-dependent expression for ssDNA persistence length determined by Tinland *et al.*<sup>19</sup>.

Here we superimpose the average predictions of  $\Delta G$  (**A, D**),  $F_{1/2}$  (**B, E**), and  $\Delta x$  (**C, F**) from each formulation on the plots from **Figures 3 and 4** corresponding to the monovalent (**A-C**) and divalent (**D-F**) titrations, respectively. The composite HEL predictions, in which all six formulations are used, are represented by solid black lines and shaded uncertainty envelopes as in **Figures 3 and 4**. Error bars and linear fits to the data are omitted for clarity.

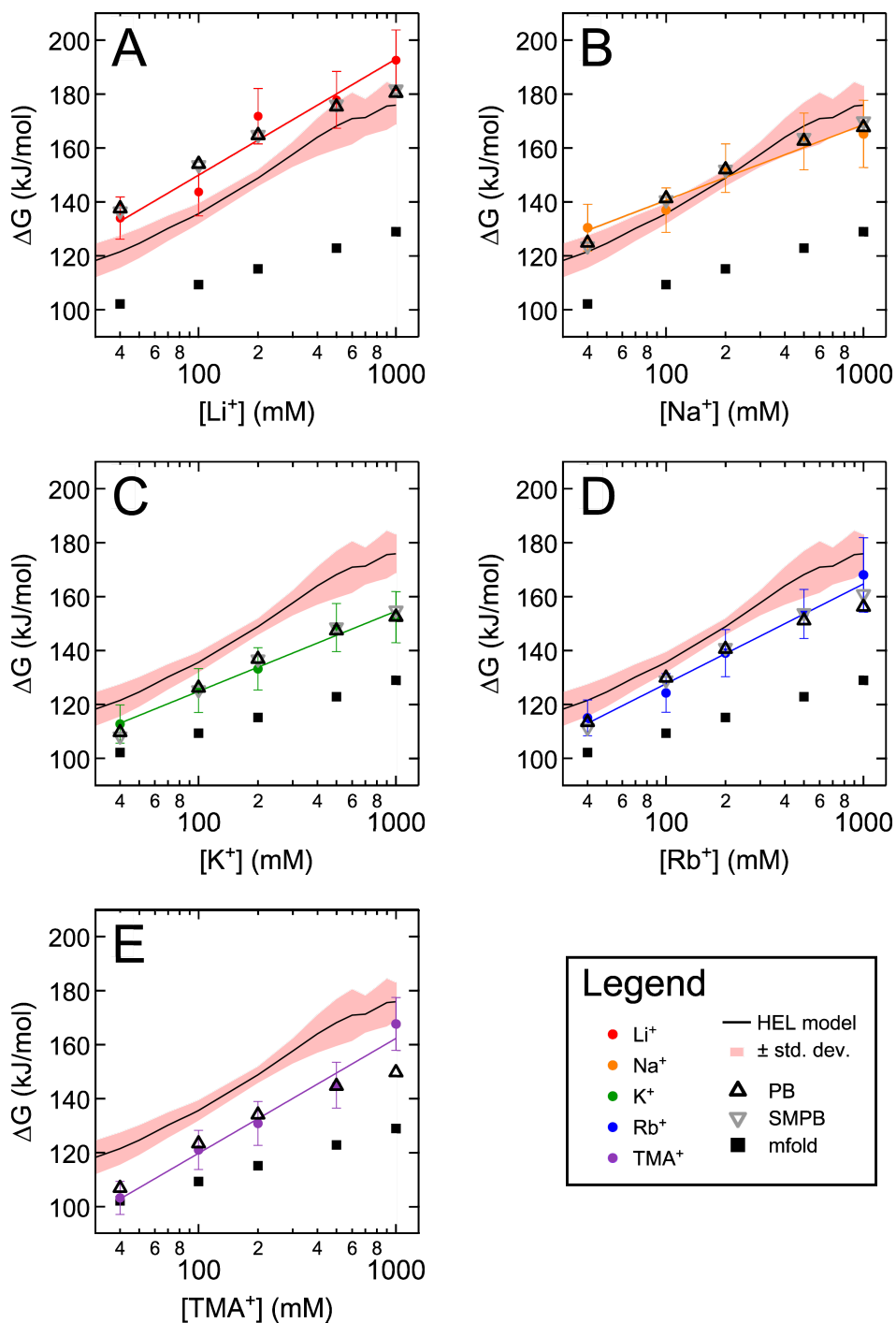
$L_{p1}$  (“Bouchiat”) is the only formulation that does not include an explicit electrostatic term.  $L_{p2}$  (“OSF”) and  $L_{p3}$  (“Marko”) vary quadratically with the Debye screening length and are colored brown in panels A-C.  $L_{p4}$  (“Thirumalai”),  $L_{p5}$  (“Dobrynin”), and  $L_{p6}$  (“Tinland”) vary linearly with the Debye screening length and are colored gray in panels A-C. The curve styles are kept consistent throughout the figure for each formulation, but in panels D-F the curves are colored to indicate  $[K^+]$ . The curves for  $L_{p4}$  stop at 600 mM  $M^+$  (A-C) because the HEL model produced numerical errors using this formulation at higher  $[M^+]$ .



**Figure S4. Thermodynamic cycle used in Poisson-Boltzmann calculations.** Each calculated electrostatic hairpin unfolding energy ( $\Delta G_{el}$ ) included the energies of solvation of the folded ( $\Delta G_F$ ) and unfolded ( $\Delta G_U$ ) hairpin models as well as the *in vacuo* Coulombic folding energy ( $\Delta G_{Coulomb}$ ). See **Experimental Section** for more information.



**Figure S5. Correlation of measured monovalent  $\Delta G$  values with  $F_{1/2}$  values, ionic radii, and competition constants.** (A) A global slope,  $m_{\text{global}} = 39 \pm 4$ , was obtained through a linear fit (not shown) to all experimental monovalent  $\Delta G$  data vs  $\log[M^+]$  (Figure 3A). This slope was used to constrain a linear fit to the  $\Delta G$  series for each ion. The  $\Delta G$  offset (left axis) was determined as the value of each individually fitted line at 300 mM  $M^+$ . Similarly, the  $F_{1/2}$  offset (right axis) for each ion equals the value at 300 mM  $M^+$  of a linear fit to the corresponding  $F_{1/2}$  data series (Figure 3C), with the slope constrained to the global value. The  $\Delta G$  and  $F_{1/2}$  offsets are thus measures of the average relative positions of the corresponding data series for each ion. Each hydrated ionic radius is the approximate distance from the ion to the oxygen atom in the first hydration shell<sup>20,21</sup> plus 1.4 Å for the water layer. (B) The same  $\Delta G$  offsets calculated in (A) are plotted against competition constants for monovalent cations measured previously<sup>22</sup>. A competition constant characterizes the displacement of one cationic species (the background counterion, here  $\text{Na}^+$ ) by another (the competing counterion, here  $\text{Li}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$  or  $\text{TMA}^+$ ) from the ion atmosphere as the bulk concentration of the competing counterion is raised. The constant is defined as the concentration of the competing counterion necessary to displace half the number of background counterions that are present in the ion atmosphere in the absence of the competing counterion. The competition constants reported here were obtained from counting ions around a DNA molecule (24-bp duplex present at <1 mM) with 50 mM background  $\text{Na}^+$  concentration. Hence, by definition, the competition constant for  $\text{Na}^+$  is 50 mM.



**Figure S6. Gallery of  $\Delta G$  values for monovalent titrations.** Experimental  $\Delta G$  (colored circles) are shown for  $\text{Li}^+$  (A),  $\text{Na}^+$  (B),  $\text{K}^+$  (C),  $\text{Rb}^+$  (D), and  $\text{TMA}^+$  (E). Energies from PB calculations (upward-pointing black triangles) were fit to each series by varying the overall offset in energy to minimize  $\chi^2$ . Similarly fitted energies from SMPB calculations (downward-pointing gray triangles) are also shown for each ion except  $\text{TMA}^+$ . Uncertainties were smaller than the symbols for both types of calculations. Each panel also includes the energies predicted by the HEL model (black curve) and *mfold* (squares) as in Figure 3.

## 3. SUPPORTING TABLES

**Table S1. Summary of HEL model predictions.**

Concentration (mM)		$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
$M^+$	$Mg^{2+}$			
40	0	$11.3 \pm 1.1$	$18.2 \pm 0.9$	$121 \pm 6$
	1	$12.2 \pm 1.1$	$18.5 \pm 0.9$	$133 \pm 6$
	2	$12.5 \pm 1.1$	$18.6 \pm 0.8$	$136 \pm 6$
	5	$12.9 \pm 1.1$	$18.6 \pm 0.8$	$141 \pm 5$
	10	$13.3 \pm 1.1$	$18.5 \pm 0.7$	$145 \pm 5$
100	0	$12.9 \pm 0.7$	$17.8 \pm 0.4$	$136 \pm 4$
200	0	$14.2 \pm 0.5$	$17.7 \pm 0.5$	$149 \pm 3$
	1	$14.5 \pm 0.5$	$17.8 \pm 0.5$	$153 \pm 3$
	2	$14.6 \pm 0.5$	$17.9 \pm 0.5$	$155 \pm 3$
	5	$14.8 \pm 0.5$	$17.9 \pm 0.5$	$157 \pm 3$
	10	$15.1 \pm 0.6$	$18.0 \pm 0.6$	$160 \pm 4$
500	0	$16.2 \pm 1.2$	$17.6 \pm 0.6$	$168 \pm 9$
1000	0	$16.7 \pm 0.9$	$17.8 \pm 0.5$	$176 \pm 7$

For each combination of  $[M^+]$  and  $[Mg^{2+}]$ , 60 calculations were conducted using different combinations of input parameters. Reported values represent the mean  $\pm$  standard deviation of outputs from all successful calculations. Calculations were also done at  $[M^+] = 30, 50, 60, 70, 80, 90, 300, 400, 600, 700, 800,$  and  $900$  mM and at  $[Mg^{2+}] = 3, 4, 6, 7, 8$  and  $9$  mM (with  $[M^+] = 40$  or  $200$  mM). All calculation results are plotted in **Figures 3 and 4**.

**Table S2. Effect of varying conditions of PB calculations on the slope ( $m_{PB}$ ) of  $\Delta G_{el}$  versus  $\log[M^+]$ .**

Electrostatic treatment in MD	PB force-field	Model type	$m_{PB}$
DC	AMBER	Standard	$32.0 \pm 1.2$
“	“	17 nm $\Delta x$	$27.8 \pm 1.5$ *
“	“	10 bp handles	$35.6 \pm 1.4$ *
“	“	5 Å/bp handle rise	$37.9 \pm 1.2$ *
“	“	No DNA handles	$30.2 \pm 1.4$ *
GB	“	Standard	$32.1 \pm 1.6$
LC	“	“	$29.4 \pm 2.8$
DC	CHARMM	“	$33.6 \pm 1.5$
GB	“	“	$33.4 \pm 1.7$
LC	“	“	$30.3 \pm 2.7$

The conditions used for the calculations reported in the main text are listed on the first row. “Standard” model denotes 25 bp handles with B-form geometry, and an 18-nm distance change ( $\Delta x$ ) between the folded and unfolded states of the hairpin. Other models are the same as the “standard” model except as noted. “\*” denotes conditions for which only 25 folded and 25 unfolded models were generated, instead of the standard 40. DC = constant dielectric of 80; GB = generalized Born<sup>23</sup>, inverse Debye-Hückel length of  $0.19 \text{ \AA}^{-1}$ ; LC = low cut-off of  $0.2 \text{ \AA}$  for long-range interactions in simulations (models were manually curated to ensure no steric clashes). The AMBER force-field was used for MD in all cases.

**Table S3. Summary of parameters for SMPB simulations of monovalent titrations.**

Ion	Ion size (Å)	$m_{SMPB}$	$\chi^2_{SMPB}$
Li <sup>+</sup>	1.00	$33.7 \pm 1.3$	2.8
Na <sup>+</sup>	7.16	$34.6 \pm 1.1$	1.0
K <sup>+</sup>	7.42	$34.9 \pm 1.1$	0.7
Rb <sup>+</sup>	9.47	$37.2 \pm 1.0$	1.1
TMA <sup>+</sup>	N.D.	N.D.	N.D.

$\Delta G_{el}$  values were calculated using the size-modified Poisson-Boltzmann algorithm<sup>9</sup> at the five experimental  $[M^+]$  values (40, 100, 200, 500 and 1000 mM) for Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup> and Rb<sup>+</sup>. Ion sizes were parameterized according to Chu, et al.<sup>9</sup>; no parameterized size was available for TMA<sup>+</sup>. A linear fit to a plot of energies versus  $\log[M^+]$  for each titration (not shown) yielded the corresponding slope ( $m_{SMPB}$ ). The energies for each titration were also fitted to the corresponding experimental  $\Delta G$  values using  $\chi^2$  minimization (with four degrees of freedom), with an energy offset as the only free parameter. The final  $\chi^2$  values ( $\chi^2_{SMPB}$ ) are reported.

The  $\Delta G_{el}$  values obtained from SMPB fit the corresponding experimental  $\Delta G$  series better in only half the cases than did the single  $\Delta G_{el}$  trend from standard PB (see also **Table 1** and **Figure S6**), indicating inconsistent improvement. The  $\Delta G_{el}$  slopes from SMPB increased with ionic radius, as was generally true for the experimental  $\Delta G$  slopes, but the differences among slopes calculated for different ions were smaller.

**Table S4. Experimental data for the Li<sup>+</sup> titration.**

Concentration (mM)	$N_{molecules}$	$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
40	7	12.6 ± 0.7	17.6 ± 0.4	134 ± 8
100	6	13.5 ± 0.8	17.6 ± 0.4	144 ± 9
200	8	16.0 ± 0.9	17.9 ± 0.4	172 ± 10
500	10	16.6 ± 0.9	17.7 ± 0.4	178 ± 11
1000	8	17.7 ± 1.0	18.1 ± 0.4	193 ± 11

**Table S5. Experimental data for the Na<sup>+</sup> titration.**

Concentration (mM)	$N_{molecules}$	$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
40	7	12.8 ± 0.8	16.9 ± 0.4	130 ± 9
100	11	13.6 ± 0.8	16.7 ± 0.4	137 ± 8
200	8	14.6 ± 0.8	17.4 ± 0.4	153 ± 9
500	10	15.4 ± 0.9	17.4 ± 0.5	162 ± 11
1000	7	15.6 ± 1.1	17.5 ± 0.4	165 ± 12

**Table S6. Experimental data for the K<sup>+</sup> titrations, in the presence and absence of Mg<sup>2+</sup>.**

Concentration (mM)		$N_{molecules}$	$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
K <sup>+</sup>	Mg <sup>2+</sup>				
40	0	9	11.2 ± 0.7	16.8 ± 0.4	113 ± 7
	1	7	12.2 ± 0.7	17.6 ± 0.4	130 ± 8
	2	7	13.9 ± 0.8	17.2 ± 0.4	144 ± 8
	5	9	14.8 ± 0.8	17.4 ± 0.4	156 ± 9
	10	10	14.9 ± 0.9	17.6 ± 0.4	159 ± 10
100	0	7	12.2 ± 0.7	17.1 ± 0.4	125 ± 8
200	0	27	13.0 ± 0.7	17.0 ± 0.4	133 ± 8
	1	8	13.9 ± 0.8	17.1 ± 0.4	143 ± 8
	2	6	14.4 ± 0.8	17.0 ± 0.4	148 ± 9
	5	12	14.6 ± 0.8	17.7 ± 0.4	156 ± 9
	10	9	14.6 ± 0.8	17.6 ± 0.4	155 ± 9
500	0	7	14.4 ± 0.8	17.1 ± 0.4	148 ± 9
1000	0	12	14.5 ± 0.8	17.4 ± 0.4	152 ± 9

**Table S7. Experimental data for the Rb<sup>+</sup> titration.**

Concentration (mM)	$N_{molecules}$	$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
40	12	11.0 ± 0.6	17.3 ± 0.4	115 ± 7
100	7	12.0 ± 0.6	17.1 ± 0.4	124 ± 7
200	9	13.4 ± 0.8	17.2 ± 0.4	139 ± 9
500	9	14.5 ± 0.8	17.6 ± 0.4	154 ± 9
1000	3	16.0 ± 1.3	17.4 ± 0.4	168 ± 14

**Table S8. Experimental data for the TMA<sup>+</sup> titration.**

Concentration (mM)	$N_{molecules}$	$F_{1/2}$ (pN)	$\Delta x$ (nm)	$\Delta G$ (kJ/mol)
40	9	10.3 ± 0.6	16.7 ± 0.4	103 ± 6
100	9	11.6 ± 0.6	17.3 ± 0.4	121 ± 7
200	10	12.4 ± 0.7	17.5 ± 0.4	131 ± 8
500	8	13.5 ± 0.7	17.8 ± 0.4	145 ± 8
1000	4	15.3 ± 0.8	18.2 ± 0.4	168 ± 10

**Tables S4-S8. Summaries of experimental data for titrations of Li<sup>+</sup> (S4), Na<sup>+</sup> (S5), K<sup>+</sup> in the presence and absence of Mg<sup>2+</sup> (S6), Rb<sup>+</sup> (S7), and TMA<sup>+</sup> (S8).** One value of each parameter ( $F_{1/2}$ ,  $\Delta x$  and  $\Delta G$ ) was calculated for each molecule measured. No molecule was measured under multiple conditions. Reported values of  $F_{1/2}$  and  $\Delta x$  represent the mean ± total propagated uncertainty, which includes the standard error on the mean (calculated by the bootstrap method) and sources of systematic uncertainty (see **Supporting Experimental Procedures**). Values of  $\Delta G$  are reported similarly, but since this parameter equals the product of  $F_{1/2}$  and  $\Delta x$ , the uncertainty in  $\Delta G$  equals the uncertainties in  $F_{1/2}$  and  $\Delta x$  added in quadrature. Relatively few molecules were measured at 1000 mM Rb<sup>+</sup> and TMA<sup>+</sup> because the high salt concentrations increased the stickiness of microscope coverslips and made it difficult to pick up dumbbells.



#### 4. SUPPORTING REFERENCES

- (1) Woodside, M. T.; Behnke-Parks, W. M.; Larizadeh, K.; Travers, K.; Herschlag, D.; Block, S. M. *Proc. Natl. Acad. Sci. U.S.A.* **2006**, *103*, 6190-5.
- (2) Gal, J.; Schnell, R.; Szekeres, S.; Kalman, M. *Mol. Gen. Genet.* **1999**, *260*, 569-73.
- (3) Spitzer, S.; Eckstein, F. *Nucleic Acids Res.* **1988**, *16*, 11691-704.
- (4) Cornell, W. D.; Cieplak, P.; Bayly, C. I.; Gould, I. R.; Merz, K. M.; Ferguson, D. M.; Spellmeyer, D. C.; Fox, T.; Caldwell, J. W.; Kollman, P. A. *J. Am. Chem. Soc.* **1995**, *117*, 5179-97.
- (5) Macke, T. J.; Case, D. A. *Molecular Modeling of Nucleic Acids* **1998**, *682*, 379-93.
- (6) Baker, N. A.; Sept, D.; Joseph, S.; Holst, M. J.; McCammon, J. A. *Proc. Natl. Acad. Sci. U.S.A.* **2001**, *98*, 10037-41.
- (7) Dong, F.; Vijayakumar, M.; Zhou, H. X. *Biophys. J.* **2003**, *85*, 49-60.
- (8) Lipfert, J.; Chu, V. B.; Bai, Y.; Herschlag, D.; Doniach, S. *J. Appl. Cryst.* **2007**, *40*, S229-34.
- (9) Chu, V. B.; Bai, Y.; Lipfert, J.; Herschlag, D.; Doniach, S. *Biophys. J.* **2007**, *93*, 3202-9.
- (10) Greenleaf, W. J.; Woodside, M. T.; Abbondanzieri, E. A.; Block, S. M. *Phys. Rev. Lett.* **2005**, *95*, 208102.
- (11) Bouchiat, C.; Wang, M. D.; Allemand, J.; Strick, T.; Block, S. M.; Croquette, V. *Biophys. J.* **1999**, *76*, 409-13.
- (12) Odijk, T. *J. Polymer Sci. B-Polymer Phys.* **1977**, *15*, 477-83.
- (13) Skolnick, J.; Fixman, M. *Macromolecules* **1977**, *10*, 944-8.
- (14) Cocco, S.; Marko, J. F.; Monasson, R.; Sarkar, A.; Yan, J. *Eur. Phys. J. E Soft Matter* **2003**, *10*, 249-63.
- (15) Marko, J. F.; Siggia, E. D. *Macromolecules* **1995**, *28*, 8759-70.
- (16) Marko, J. F., Personal communication **2009**.
- (17) Ha, B. Y.; Thirumalai, D. *Macromolecules* **1995**, *28*, 577-81.
- (18) Dobrynin, A. V. *Macromolecules* **2005**, *38*, 9304-14.
- (19) Tinland, B.; Pluen, A.; Sturm, J.; Weill, G. *Macromolecules* **1997**, *30*, 5763-5.
- (20) Garde, S.; Hummer, G.; Paulaitis, M. E. *J. Chem. Phys.* **1998**, *108*, 1552-61.
- (21) Ohtaki, H.; Radnai, T. *Chem. Rev.* **1993**, *93*, 1157-204.
- (22) Bai, Y.; Greenfeld, M.; Travers, K. J.; Chu, V. B.; Lipfert, J.; Doniach, S.; Herschlag, D. *J. Am. Chem. Soc.* **2007**, *129*, 14981-8.
- (23) Tsui, V.; Case, D. A. *Biopolymers* **2000**, *56*, 275-91.